



## Investigation on Sine functions

**Objective:** In this investigation we will examine the features of sine function with its transformation.

*Use of Graphing calculator is required for this activity (Casio cg20 or Casio cg50 is recommended)*

- Sketch the following curves for  $f(x) = a \sin x$  using your GDC and fill the table that follow.

- a.  $y_1 = \sin x$
- b.  $y_2 = 2 \sin x$
- c.  $y_3 = 0.5 \sin x$
- d.  $y_4 = -\sin x$
- e.  $y_5 = -2 \sin x$

<b><math>a</math></b>	<b><math>f(x)</math></b>	<b>Maximum value</b>	<b>Minimum value</b>	<b>Amplitude = <math>\frac{\max - \min}{2}</math></b>	<b>Period</b>
1	$\sin x$				
2	$2 \sin x$				
0.5	$0.5 \sin x$				
-1	$-\sin x$				
-2	$-2 \sin x$				

What is the effect of  $a$  in  $f(x) = a \sin x$ ?

- Sketch the following curves for  $f(x) = \sin bx$  using your GDC and fill the table that follow.

- a.  $y_1 = \sin x$
- b.  $y_2 = \sin 2x$
- c.  $y_3 = \sin 0.5x$
- d.  $y_4 = \sin 0.25x$

<b><math>b</math></b>	<b><math>f(x)</math></b>	<b>Maximum value</b>	<b>Minimum value</b>	<b>Amplitude = <math>\frac{\max - \min}{2}</math></b>	<b>Period</b>
1	$\sin x$				
2	$\sin 2x$				
0.5	$\sin 0.5x$				





0.25	$\sin 0.25x$				
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What is the effect of  $b$  in  $f(x) = \sin bx$ ?

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3. Sketch the following curves for  $f(x) = \sin(x - c)$  using your GDC and fill the table that follow.

- a.  $y_1 = \sin x$
- b.  $y_2 = \sin(x - 1)$
- c.  $y_3 = \sin(x + 1)$
- d.  $y_4 = \sin(x - \frac{\pi}{2})$

<b><math>c</math></b>	<b><math>f(x)</math></b>	<b>Maximum value</b>	<b>Minimum value</b>	<b>Amplitude = <math>\frac{\max - \min}{2}</math></b>	<b>Period</b>
0	$\sin x$				
1	$\sin(x - 1)$				
-1	$\sin(x + 1)$				
$\frac{\pi}{2}$	$\sin(x - \frac{\pi}{2})$				

What is the effect of  $c$  in  $f(x) = \sin(x - c)$ ?

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4. Sketch the following curves for  $f(x) = \sin x + d$  using your GDC and fill the table that follow.

- a.  $y_1 = \sin x$
- b.  $y_2 = \sin x + 1$
- c.  $y_3 = \sin x + 2$
- d.  $y_4 = \sin x - 2$

<b><math>d</math></b>	<b><math>f(x)</math></b>	<b>Maximum value</b>	<b>Minimum value</b>	<b>Amplitude = <math>\frac{\max - \min}{2}</math></b>	<b>Period</b>
1	$\sin x$				
2	$\sin x + 1$				
0.5	$\sin x + 2$				
0.25	$\sin x - 2$				

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Page 2 of 3





What is the effect of  $d$  in  $f(x) = \sin x + d$ ?

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Summarize your findings about  $a, b, c$  and  $d$  in  $f(x) = a\sin(bx - c) + d$

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