

# VARIABLE MEMORIES & SOLVING EQUATIONS USING A CASIO SCIENTIFIC CALCULATOR

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Adequate knowledge of calculator skills makes the teaching of Financial Maths & Functions easier and enables the educator to assist their learners more efficiently.

**Content:** This workshop will cover: In-putting values into the CASIO calculator MEMORY, using the saved values & recalling what has been saved. Using TABLE MODE – solving Simultaneous, Quadratic & Cubic equations.

## Worksheet:

## VARIABLE MEMORIES



To assign the result of $3 + 5$ to variable A	<b>3</b> <b>+</b> <b>5</b> <b>SHIFT</b> <b>RCL</b> <b>(-)</b>
To multiply the contents of variable A by 10	<b>ALPHA</b> <b>(-)</b> <b>X</b> <b>1</b> <b>0</b> <b>=</b>
To recall the contents of variable A	<b>RCL</b> <b>(-)</b>

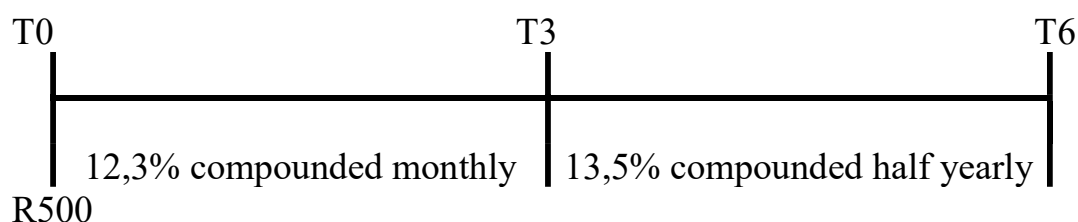
On the calculator, financial maths calculations are done as a continuous calculation.

If you use the memory keys, you do not have to key in the same numbers repeatedly.

Which helps save time and prevent confusion.

### Example 1

What would an investment of R500 be worth in 6 years' time, if for the first 3 years it earns 12,3% p.a. compounded monthly and for the last 3 years it earns 13,5% p.a. compounded half-yearly?



$$A = P(1 + i)^n$$

$$A = 500 \left(1 + \frac{0.123}{12}\right)^{3 \times 12} \left(1 + \frac{0.135}{2}\right)^{3 \times 2}$$

STORE:  $\left(1 + \frac{0.123}{12}\right)$  INTO VARIABLE A [SHIFT] [RCL] [(-)]

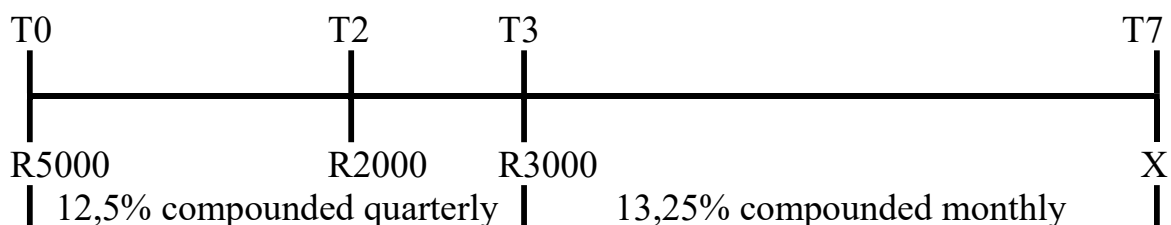
STORE:  $\left(1 + \frac{0.135}{2}\right)$  INTO VARIABLE B [SHIFT] [RCL] [0,9]

And then complete the calculation

[5] [0] [0] [ALPHA] [(-)] [x^y] [3] [X] [1] [2] [▶] [ALPHA] [0,9] [x^y] [3] [X]  
[2]

### Example 2

A man borrows R5 000 and agrees to repay the amount as follows: R2 000 after 2 years, R3 000 after 3 years and the balance at the end of 7 years. How much must he pay if interest is at 12,5% p.a. compounded quarterly for the first three years and 13,25% p.a. compounded monthly thereafter?



$$A = P(1 + i)^n$$

$$0 = 5000 \left(1 + \frac{0.125}{4}\right)^{3 \times 4} \left(1 + \frac{0.1325}{12}\right)^{4 \times 12} - 2000 \left(1 + \frac{0.125}{4}\right)^{1 \times 4} \left(1 + \frac{0.1325}{12}\right)^{4 \times 12} - 3000 \left(1 + \frac{0.1325}{12}\right)^{4 \times 12} - X$$

STORE:  $\left(1 + \frac{0.125}{4}\right)$  INTO VARIABLE A [SHIFT] [RCL] [(-)]

STORE:  $\left(1 + \frac{0.1325}{12}\right)$  INTO VARIABLE B [SHIFT] [RCL] [0,.,"]

And then complete the calculation

[5] [0] [0] [0] [ALPHA] [(-)] [x^n] [3] [X] [4] [▶] [ALPHA] [0,.,"] [x^n] [4] [X]  
 [1] [2] [▶] [-] [2] [0] [0] [0] [ALPHA] [(-)] [x^n] [1] [X] [4] [▶] [ALPHA]  
 [0,.,"] [x^n] [4] [X] [1] [2] [▶] [-] [3] [0] [0] [0] [ALPHA] [0,.,"] [x^n] [4]  
 [X] [1] [2] [=]

- The Memory Keys save time – less calculator keys are pressed.
- The Memory Keys do not have to be cleared to be used again. When saving a new value, it overwrites the existing value.

## MODE 3: Table

Find the points of intersection of the straight line  $f(x) = x - 3$  and the parabola  $g(x) = x^2 - x - 6$  when  $x \in [-3 ; 4]$

Key Sequence:

- Input  $f(x)$  formula  $\boxed{=}$
- Input  $g(x)$  formula  $\boxed{=}$
- Set boundaries for the table:  
 Start?  $\boxed{(-)} \boxed{3} \boxed{=}$   
 End?  $\boxed{4} \boxed{=}$   
 Step?  $\boxed{1} \boxed{=}$

Point of Intersection (-1 ; -4)

Point of Intersection (3 ; 0)

On screen:

$$f(X)=X-3$$

$$g(X)=X^2-X-6$$

X	F(X)	G(X)
-3	-6	-6
-2	-5	-4
-1	-4	-4

X	F(X)	G(X)
0	-3	-6
1	-2	-6
2	-1	-4

X	F(X)	G(X)
3	0	0
4	1	6

**\* ZOOM IN \*** and find the turning point of  $g(x)$

Key Sequence:

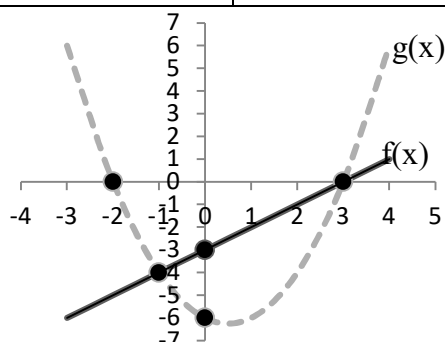
- $\boxed{AC}$
- Change the boundaries of the table  
 Start?  $\boxed{0} \boxed{=}$   
 End?  $\boxed{1} \boxed{=}$   
 Reduce the  
 STEPS/INTERVALS for a  
 more detailed table.  
 Step?  $\boxed{\cdot} \boxed{2} \boxed{5} \boxed{=}$

Turning point of  $g(x)$ : (0,5 ; -6,25)

On screen:

X	F(X)	G(X)
0	-3	-6
0.25	-2.75	-6.187
0.5	-2.5	-6.25

X	F(X)	G(X)
0.75	-2.25	-6.187
1	-2	-6



# SOLVING EQUATIONS

## 1. Simultaneous equations with 2 unknowns

**Solve for  $x$  and  $y$ :**

$$3x + 2y = -8$$

$$5x - 4y = -6$$

Manipulate

$$y = \frac{-3x - 8}{2}$$

$$y = \frac{5x + 6}{4}$$

### Key Sequence:

- Input  $f(x)$  formula  $\boxed{=}$
- Input  $g(x)$  formula  $\boxed{=}$
- Set boundaries for the table:

Start?  $\boxed{=}$   $\boxed{9}$   $\boxed{=}$

End?  $\boxed{9}$   $\boxed{=}$

Step?  $\boxed{1}$   $\boxed{=}$

$x = -2$  and  $y = -1$

### On screen:

$$f(X) = \frac{-3X - 8}{2}$$

$$g(X) = \frac{5X + 6}{4}$$

X	F(X)	G(X)
-2	-2.5	-2.25
-1	-1	-1
0	0.5	-0.25
1	1	0.25

*DON'T FORGET*

$f(x)$  &  $g(x)$  – 20  $x$  values

$f(x)$  – 30  $x$  values

*HOW TO CHANGE:*

1:ab/c 2:d/c  
3:STAT 4:TABLE  
5:Disp 6:APO  
7:CONT

Select Type?  
1: f(x)  
2: f(x), g(x)

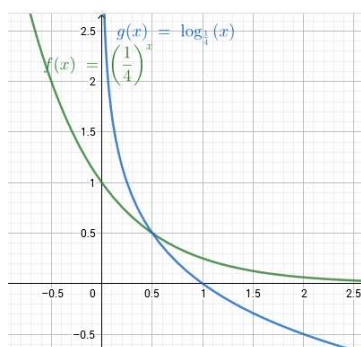
4

Now try:  $\left(\frac{1}{4}\right)^x = \log_{\frac{1}{4}} x$

Start: 0

End: 9

Steps: 0,5

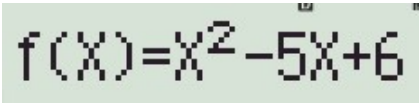
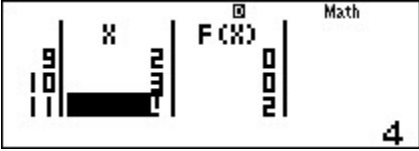


X	F(X)	G(X)
0.5	0.5	0.5
1	0.25	0.25
1.5	0.125	0.125
2	0.0625	0.0625
2.5	0.03125	0.03125

## 2. Quadratic equation

Generate a TABLE for the equation & read off the  $x$  value where  $f(x) = 0$

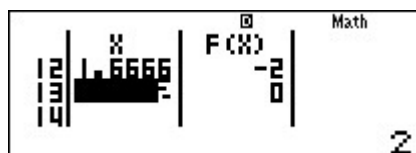
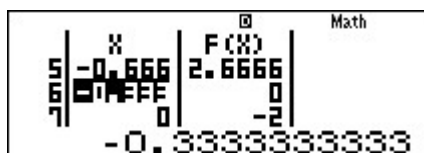
$$x^2 - 5x + 6 = 0$$

<p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>Input <math>f(x)</math> equation <math>\equiv</math>  <b>to input the variable <math>x</math>:</b>  <math>\boxed{\text{ALPHA}} \boxed{\square}</math></li> <li><math>g(x) = \equiv</math></li> <li>Set boundaries for your table:  <b>Start?</b> <math>\boxed{-} \boxed{6} \boxed{=}</math>  <b>End?</b> <math>\boxed{6} \boxed{=}</math>  <b>Step?</b> <math>\boxed{1} \boxed{=}</math></li> </ul> <p><math>f(x) = 0</math> at <math>x = 2</math> or <math>x = 3</math></p>	<p><b>On screen:</b></p>  
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**DOMAIN:** Negative & positive values of the constant

**STEPS:** Reciprocal of the co-efficient of the highest power of  $x$

Now try:  $3x^2 - 5x = 2$



## 3. Cubic equation

Generate a TABLE for the equation & read off the  $x$  value where  $f(x) = 0$

$$2x^3 + 3x^2 - 11x - 6 = 0$$

### Key Sequence:

- Input  $f(x)$  equation  $\boxed{=}$
- $g(x) = \boxed{=}$
- Set boundaries for your table:

Start?  $\boxed{-}$   $\boxed{6}$   $\boxed{=}$

End?  $\boxed{6}$   $\boxed{=}$

Step?  $\boxed{1}$   $\boxed{\div}$   $\boxed{2}$   $\boxed{=}$

- Turn  $g(x)$  off

$\boxed{\blacktriangleright}$   $\boxed{\text{SHIFT}}$   $\boxed{\text{MODE}}$   $\boxed{\blacktriangledown}$   $\boxed{4}$   $\boxed{1}$

$f(x) = 0$  at

$$x = -3 \text{ or } x = -\frac{1}{2} \text{ or } x = 2$$

### On screen:

$$f(X) = X^2 - 11X - 6$$

Insufficient MEM  
[AC] : Cancel  
[←][→]: Goto

X	F(X)
-3.5	-16.5
-2.5	9

-3

X	F(X)
-1	6
-0.5	-6

-0.5

X	F(X)
1.5	-9
2.5	16.5

2

Now try:  $x^3 - \frac{3}{2}x^2 - 4x + 6 = 0$

X	F(X)
1.5	3
2	0

1.5

X	F(X)
-2.5	-18
-1.5	10.5

-2

X	F(X)
1.5	0
2.5	4.5

2

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